

## pp-definability is *NEXPTIME*-complete

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ROSS WILLARD

*Department of Pure Mathematics, Univeristy of WATERLOO*  
rdwillar@uwaterloo.ca

It is known (Friedman, unpublished; Bergman, Jeudes and Slutzki, IJAC '99) that the clone membership problem for finite algebras is *EXPTIME*-complete. The analogous *relational clone membership problem* for finite relational structures, also called  $\exists$ -INVSAT in the theoretical computer science community, is the problem which accepts as input a finite set  $\mathcal{R}$  of finitary relations on a finite set  $A$ , together with another relation  $s$  on  $A$ , and asks if  $s$  is in the relational clone  $\text{Inv}(\text{Pol}(\mathcal{R}))$  generated by  $\mathcal{R}$ . We show that this problem is *NEXPTIME*-complete.