Institute of Mathematics, Czech Academy of Sciences, Czech Republic bartos@math.cas.cz

Hereditarily indecomposable continua as Fraïssé limits

Joint work with Wiesław Kubiś

In 2006, Irwin and Solecki introduced projective Fraïssé theory of topological structures and showed that a pre-space of the pseudo-arc is the Fraïssé limit of the class of all finite linear graphs and quotient maps. They also characterized the pseudo-arc as the unique arc-like continuum \mathbb{P} such that for every arc-like continuum Y, every $\varepsilon > 0$, and every continuous surjections $f, g: \mathbb{P} \to Y$ there is a homeomorphism $h: \mathbb{P} \to \mathbb{P}$ such that $\sup_{x \in \mathbb{P}} d(f(x), g(h(x))) < \varepsilon$.

We consider an approximate framework for Fraïssé theory where the pseudo-arc itself is the Fraïssé limit of the category \mathcal{I} of all continuous surjections of the unit interval, in the category $\sigma \mathcal{I}$ of all arc-like continua and all continuous surjections. The characterizing condition above becomes the *projective homogeneity* condition in our framework.

Similarly, we may consider the category S of all continuous surjections of the unit circle, and the category σS of all circle-like continua and all continuous surjections. It turns out there is no Fraïssé limit of S in σS . However, if we restrict to the subcategory $S_P \subseteq S$ of the maps whose degree uses only primes from a fixed set P, and the subcategory $\sigma S_P \subseteq \sigma S$ of circle-like continua that are limits of inverse sequences of S_P -maps, with maps that can be approximated by S_P -maps as morphisms, then the corresponding Fraïssé limit is the P-adic pseudo-solenoid \mathbb{P}_P , and it is characterized as the unique σS_P -object that is *projectively homogeneous*, or equivalently has the *projective extension property*.